

3.7 Products. Sums. Linear Combinations. and

10. Derive a formula for $\tan 4x$.

$$\begin{aligned}
 \tan 4x &= \tan(2x + 2x) \\
 &= \frac{\tan 2x + \tan 2x}{1 - \tan 2x \tan 2x} \\
 &= \frac{2 \tan 2x}{1 - \tan^2 2x} \\
 &= \frac{2 \cdot \frac{2 \tan x}{1 - \tan^2 x}}{1 - \left(\frac{2 \tan x}{1 - \tan^2 x}\right)^2} \\
 &= \frac{4 \tan x}{1 - \tan^2 x} \div \frac{(1 - \tan^2 x)^2 - 4 \tan^2 x}{(1 - \tan^2 x)^2} \\
 &= \frac{4 \tan x}{1 - \tan^2 x} \div \frac{1 - 2 \tan^2 x + \tan^4 x - 4 \tan^2 x}{(1 - \tan^2 x)^2} \\
 &= \frac{4 \tan x}{1 - \tan^2 x} \cdot \frac{(1 - \tan^2 x)^2}{1 - 6 \tan^2 x + \tan^4 x} \\
 &= \frac{4 \tan x - 4 \tan^3 x}{1 - 6 \tan^2 x + \tan^4 x}
 \end{aligned}$$

11. Let $y = 0$.

$$\begin{aligned}
 3.50 \sin t + 1.20 \sin 2t &= 0 \\
 3.50 \sin t + 2.40 \sin t \cos t &= 0, \text{ Double-Angle Identity} \\
 \sin t(3.50 + 2.40 \cos t) &= 0 \\
 \sin t = 0 \text{ or } 3.50 + 2.40 \cos t &= 0 \\
 2.40 \cos t &= -3.50 \\
 \cos t = -1.46 &\rightarrow \text{no solution because } -1 \leq \cos t \leq 1. \\
 t &= 0, \pi
 \end{aligned}$$