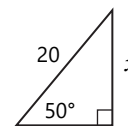


LESSON 90

- B, D, F
A is false because the rays have different endpoints. C is false because two points determine a line. E is false because the supplement of an acute angle is obtuse.
- B, C
- A; The first step is to add 4 to both sides.
- Use the Segment Addition Postulate [7.6].
 $AP + PB = AB$
 $2x + (3x - 2) = 18; x = 4$
 $AP = 2(4) = 8$
 $PB = 3(4) - 2 = 10$
- Angles in a triangle add up to 180° .
 $x + 2x + 3x = 180$
 $x = 30$
The triangle has angles measuring 30° , 60° , and 90° , so it is a right triangle.
- Angles in a triangle add up to 180° .
 $m\angle BCA = 180 - 90 - 58 = 32^\circ$
If lines are parallel, then alternate interior angles are congruent.
 $m\angle 1 = m\angle BCA = 32^\circ$
- B
3. All right angles are congruent.
4. If corresponding angles are congruent, then lines are parallel.
- A; A maps the point to $(1, -1)$. B, C, and D map the point to $(-1, -1)$.
- Assume that n is odd.
- interior angle sum of a hexagon = $180(6 - 2) = 720^\circ$
- A; $2 + 4 > 8$ is false. The sum of two sides of a triangle must be greater than the third side.
- D; The included angles must be congruent.
- Use the Leg Rule [68.2].
 $12^2 = 6(6 + x)$
 $x = 18$
- C; $\tan 60^\circ = \sqrt{3}$
- Corresponding sides must be proportional.
 $\frac{16}{16 + 8} = \frac{x}{x + 7} \rightarrow 16(x + 7) = 24x \rightarrow x = 14$
 $\frac{16}{16 + 8} = \frac{10}{y} \rightarrow 16y = 24(10) \rightarrow y = 15$

- A diagonal divides a rhombus into two congruent isosceles triangles with congruent base angles.
 $m\angle 1 = 62^\circ$
Angles in a triangle add up to 180° .
 $m\angle 2 = 180 - 62 - 62 = 56^\circ$
- In a parallelogram, opposite angles are congruent, and consecutive angles are supplementary.
Let $4x$ and $5x$ be the two angles.
 $4x + 5x = 180; x = 20$
The angles are 80° , 100° , 80° , and 100° .
- D; The quadrilateral is a parallelogram because opposite sides are congruent. A rhombus is a parallelogram with perpendicular diagonals.
- A centroid divides a median in the ratio 2:1.
 $AP = 2PD$
 $3x - 4 = 2x; x = 4$
 $AD = AP + PD = 8 + 4 = 12$
- B, C, D, E
- B
3. If lines are parallel, then alternate interior angles are congruent.
4. Reflexive Property
5. ASA
- A midsegment is half the length of the third side.
perimeter of $\triangle STU = ST + TU + SU$
 $= XZ/2 + XY/2 + YZ/2$
 $= 15 + 13 + 12 = 40$
- The midsegment is half the sum of the bases.
 $MN = (PQ + SR)/2$
 $7 = (5 + SR)/2$
 $SR = 9$
- Angles in a triangle add up to 180° .
 $m\angle Z = 180 - 55 - 65 = 60^\circ$
The larger angle has the longer opposite side.
 $YZ < XY < XZ$ because $m\angle X < m\angle Z < m\angle Y$.
- C
- The triangle is obtuse because $11^2 > 7^2 + 8^2$.
- $\sin 50^\circ = x/20$
 $x = 20 \sin 50^\circ \approx 15.3$
The top of the ladder reaches about 15.3 ft high.
- $\frac{5}{h} = \frac{8}{24} \rightarrow 8h = 5(24) \rightarrow x = 15$
The tree is 15 ft tall.



LESSON 132

- slope $m = (6 - 4)/(3 - 2) = 2$
 point-slope form: $y - 4 = 2(x - 2)$
 slope-intercept form: $y = 2x$
- Add the two equations to get $3x = 6$ and $x = 2$.
 Use the first equation to get $2 - y = 3$ and $y = -1$.
 So, the lines intersect at $(2, -1)$.
- | | |
|----------------------|---------------------------|
| By factoring: | By completing the square: |
| $x^2 + 2x - 3 = 0$ | $x^2 + 2x + 1 = 3 + 1$ |
| $(x - 1)(x + 3) = 0$ | $(x + 1)^2 = 4$ |
| $x = 1, x = -3$ | $x + 1 = 2, x + 1 = -2$ |
| | $x = 1, x = -3$ |
-
- Use the Angle Addition Postulate [7.7].
 $m\angle XOY + m\angle YOZ = m\angle XOZ$
 $2m\angle YOZ + m\angle YOZ = 150^\circ$
 $m\angle YOZ = 50^\circ$
- | | |
|----------------------|------------------------------|
| complementary angles | 7. alternate interior angles |
| $2x + x = 90$ | $5x + 6 = 116$ |
| $x = 30$ | $x = 22$ |
- | | |
|--------------------------------|---------------------------|
| 8. \triangle angle sum = 180 | 9. quad. angle sum = 360 |
| $x + 100 + 46 = 180$ | $5x + 4x + 5x + 4x = 360$ |
| $x = 34$ | $x = 20$ |
- interior angle sum = $180(n - 2) = 180(5 - 2) = 540^\circ$
 one interior angle = $540/5 = 108^\circ$
 exterior angle sum of any polygon = 360°
 one exterior angle = $360/5 = 72^\circ$
- interior angle sum = one interior angle $\times n$
 $180(n - 2) = 135n; n = 8$
 The polygon has 8 sides.
12. $(-3, -4)$
13. $(-4, 2)$
- a rotation of 180° about the origin; A composition of reflections over two intersecting lines is a rotation.
- 11111
- Answers may vary. Sample(s):
 two equilateral triangles with different side lengths
- If two segments are congruent, then they have the same length.
 If two segments have the same length, then they are congruent.
- If a figure is a rhombus, then it is a quadrilateral.
- Substitution Property
- Transitive Property

- Addition Property; Add 7 to both sides.
- Assume that $\angle 1$ and $\angle 2$ are both right angles.
- $\triangle PEF \cong \triangle PGH$ by SAS.
- There is not enough information.
- | |
|--|
| 2. Alternate interior \angle s on parallel lines are \cong . |
| 3. ASA |
| 4. CPCTC |
- $\triangle DEF$ is equilateral and thus equiangular, so $a = 60$.
 $\triangle DFG$ is isosceles with $m\angle DFG = 120^\circ$, so $b = 30$.
- $\triangle RSV$ is isosceles, so $a = m\angle V = 40$.
 $\triangle RTU$ is isosceles with vertex angle 46° , so $b = 67$.
 c is an exterior angle of $\triangle RTU$, so $c = 46 + b = 113$.