

LESSON 82

1. $3 \times 4 - (6 - 2)^2 \div 8$

$$\begin{aligned} &= 3 \times 4 - 4^2 \div 8 && \text{Parentheses} \\ &= 3 \times 4 - 16 \div 8 && \text{Exponents} \\ &= 12 - 16 \div 8 && \text{Multiplication} \\ &= 12 - 2 && \text{Division} \\ &= 10 && \text{Subtraction} \end{aligned}$$

2. $3(x - 2) + 2a = a - x$

$$\begin{aligned} 3(x - 2) + 2(2) &= 2 - x && \text{Plug in } a = 2. \\ 3x - 6 + 4 &= 2 - x && \text{Simplify each side.} \\ 3x - 2 &= 2 - x && \text{Add } x \text{ to both sides.} \\ 4x - 2 &= 2 && \text{Add 2 to both sides.} \\ 4x &= 4 && \text{Divide both sides by 4.} \\ x &= 1 \end{aligned}$$

3. $\frac{1}{6} + \frac{1}{4}x = \frac{1}{3}x$

$$\begin{aligned} 2 + 3x &= 4x && \text{Multiply both sides by 12.} \\ 2 - x &= 0 && \text{Subtract } 4x \text{ from both sides.} \\ -x &= -2 && \text{Subtract 2 from both sides.} \\ x &= 2 && \text{Divide both sides by } -1. \end{aligned}$$

4. The answer is B.

A) $2x = 4$	B) $0 = 7$
$x = 2$	No solution
C) $-1 = -1$	D) $2x = 0$
True for all x	$x = 0$

5. The answers are A and B.

A) $9 - 2(0) > (0) + 3$	B) $9 - 2(1) > (1) + 3$
$9 > 3$	$7 > 4$
Solution	Solution
C) $9 - 2(2) > (2) + 3$	D) $9 - 2(3) > (3) + 3$
$5 > 5$	$3 > 6$
Not a solution	Not a solution

6. $3 \leq 3 - 4x < 5$

$$\begin{aligned} 0 &\leq -4x < 2 && \text{Subtract 3 from all sides.} \\ 0 &\geq x > -\frac{1}{2} && \text{Divide all sides by } -4 \text{ and} \\ &&& \text{flip the inequality sign.} \\ -\frac{1}{2} &< x \leq 0 && \text{Write in ascending order.} \end{aligned}$$

7. $2|x + 1| - 5 = 3$

$$\begin{aligned} 2|x + 1| &= 8 && \text{Isolate the absolute value.} \\ |x + 1| &= 4 && \text{Rewrite as two equations.} \\ x + 1 &= 4 \text{ or } x + 1 = -4 \\ x &= 3, x = -5 && \text{Solve each equation.} \end{aligned}$$

The positive solution is 3.

8. The answer is A.

Isolate the absolute value and you get $|x| \leq -1$. This inequality has no solutions because an absolute value can never be negative.

9. Let $x = \text{regular price}$

$0.2x = \text{amount of discount}$

$\text{Sale price} = \text{regular price} - \text{amount of discount}$, so $x - 0.2x = 24$.

Solve for x , and you get $x = 30$.

The regular price was \$30.

10. Let $x = \text{Carol's age now}$

$x + 7 = \text{Victor's age now}$

$x - 3 = \text{Carol's age 3 years ago}$

$(x + 7) - 3 = \text{Victor's age 3 years ago}$

$\text{Victor's age 3 years ago} = \text{twice Carol's age 3 years ago}$, so $(x + 7) - 3 = 2(x - 3)$.

Solve for x , and you get $x = 10$.

Carol is 10 years old. Victor is 17 years old.

11. Let $x = \text{score of the fourth quiz}$

$\text{Average} = (\text{sum of four scores})/4 \geq 90$, so $(90 + 84 + 92 + x)/4 \geq 90$.

Solve for x , and you get $x \geq 94$.

Scott must score at least 94 points.

12. $m = \frac{4 - (-2)}{2 - 0} = 3$ Find the slope using the slope formula.

$b = -2$ $(0, -2)$ is the y -intercept.

$y = mx + b$ Slope-intercept form

$y = 3x - 2$ Plug in m and b .

13. The answer is D.

Lines parallel to the x -axis are horizontal lines.

Horizontal lines have an equation of the form $y = k$ where k is a constant.

14. The slope of the given line is -2 . The slope of the parallel line is also -2 because parallel lines have the same slope. The y -intercept is 3.

$y = mx + b$ Slope-intercept form

$y = -2x + 3$ Plug in m and b .

$-1 = -2k + 3$ Plug in $(k, -1)$.

$k = 2$ Solve for k .

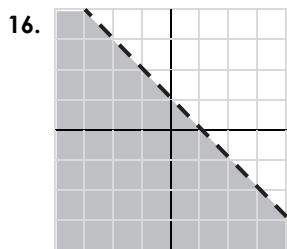
15. Convert $x - 3y = 6$ to slope-intercept form and you get $y = (1/3)x - 2$. The slope of the given line is $1/3$.

The slope of the perpendicular line is -3 because perpendicular lines have the slopes that are opposite (negative) reciprocals of each other.

$y - y_1 = m(x - x_1)$ Point-slope form

$y + 2 = -3(x - 1)$ Plug in m and $(1, -2)$.

$y = -3x + 1$ Slope-intercept form



x -intercept: $(1, 0)$
 y -intercept: $(0, 1)$

17. The answer is B.

A) Has vertex $(0, -2)$. B) Has vertex $(2, 0)$.
 C) Has vertex $(0, 2)$. D) Has vertex $(-2, 0)$.

18. The answer is C.

The initial value is 30,000 and the rate of change is $-1,200$, so the equation is $y = 30000 - 12000x$

19. $4x$ = number of seats from 4-seat tables

$6x$ = number of seats from 6-seat tables

Total number of seats = 88, so $4x + 6y = 88$.

Given $y = 8$, $4x + 6(8) = 88$.

Solve for x , and you get $x = 10$.

There are 10 4-seat tables.

20. Let x = width of the pen

Perimeter = $2(\text{width} + \text{length}) \leq 200$,
 so $2(x + 60) \leq 200$.

Solve for x , and you get $x \leq 40$.

The maximum possible width is 40 feet.

21. $1 < x < 3$

Solve the first inequality.

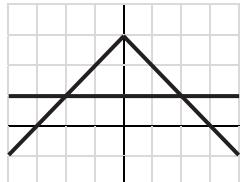
$-6 < y < -1$

Solve the second inequality.

$-5 < x + y < 2$

Add the inequalities.

22.



$$\begin{aligned} \text{Area} &= \frac{1}{2}(\text{base})(\text{height}) \\ &= \frac{1}{2}(4)(2) = 4 \end{aligned}$$

The area is 4 square units.